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S.E. (E&TC/Electronics Engg.) (II Sem.) EXAMINATION, 2017 FINGINEERING MATHEMATICS-III

(2015 PATTERN)

Time : Two Hours

Maximum Marks: 50

N.B. :— (i) Answer Q. No. 1 or Q. No. 2, Q. No. 3 or Q. No. 4, Q. No. 5 or Q. No. 6, Q. No. 7 or Q. No. 8.

- (ii) Neat diagrams must be drawn wherever necessary.
- (iii) Figures to the right indicate full marks.
- (iv) Use of logarithm's tables, slide rule, Mollier charts, electronic pocket calculator and steam tables is allowed.
- (v) Assume suitable data, if necessary.
- 1. (a) Solve any two
 - (i) $(D^2 7D + 6)y = e^{2x}$
 - $(ii) \quad (D^2 + 4)y = x \sin x$
 - (iii) $(x+2)^2 \frac{d^2y}{dx^2} + 3(x+2) \frac{dy}{dx} + y = 4 \sin \log (x+2)$.
 - (b) Find the Fourier sine transform of the function: [4]

$$f(x) = e^{-x}, \ x > 0.$$



- 2. (a) A circuit consists of an inductance L and condenser of capacity C in series. An alternating e.m.f. E sin nt is applied to it at time t = 0, the initial current and charge on the condenser being zero and w² = 1/LC, find the current flowing in the circuit at any time for w≠n. [4]
 - (b) Find inverse z-transform (any one): [4]

(i)
$$F(z) = \frac{z}{(z-1)(z-3)}, |z| > 3$$

(ii)
$$F(z) = \frac{z}{\left(z - \frac{1}{4}\right)\left(z - \frac{1}{5}\right)}.$$

(by inversion integral method).



3. (a) Using fourth order Runge-Kutta method, solve the differential equation : [4]

$$\frac{dy}{dx} = x + y + xy$$

with y(0) = 1 to get y(0.1) taking h = 0.1.

(c)





the directional derivative of : (c)

$$\phi = x^2 - y^2 + 2z^2$$

the point (1, 2, 3) in the direction of $4\overline{i} - 2\overline{j} + \overline{k}$.

Show that (any one):

Show that :



- (ii) $\nabla \left(\overline{a} \cdot \nabla \frac{1}{r} \right) = \underbrace{3(\overline{a} \cdot \overline{r})\overline{r}}_{n^{5}} \underbrace{\overline{a}}_{n^{3}}$
- $\vec{F} = (6xv + z^3)\vec{i} + (3x^2 z)\vec{i} + (3xz^2 v)\vec{k}$

is irrotational. Find scalar potential ϕ such that \overline{F} =

By using Trapezoidal rule, evaluate [4] (c)

$$\int_0^2 \frac{1}{1+x^4} dx$$

taking $h = \frac{1}{2}$, correct upto 3-decimal places.

(b)

[4]

Evaluate $\int \overline{F} \cdot d\overline{r}$ for 5.

$$\overline{F} = 3x^2 \overline{i} + (2xz - y)\overline{j} + z\overline{k}$$

along straight line joining (0, 0, 0) and (2, 1, 3).

Evaluate: (b) [4]

[4]

[5]

$$\iint \left[(4x + 3yz^2)\overline{i} - (x^2z^2 + y)\overline{j} + (y^2 + 2z)\overline{k} \right] . d\overline{S}$$

where S is the surface of the sphere $x^2 + y^2 + z^2 = 9$.

Apply Stokes' theorem to evaluate $\oint \overline{F} d\overline{r}$ where :

$$\overline{F} = xy^2 \, \overline{i} + y \overline{j} + z^2 \overline{k}$$

and C is the boundary of rectangle :

- x = 0, y = 0, x = 1, y = 2 in z = 0 plane.
- Using Green's lemma evaluate : 6. (a)

$$\int_{\mathbb{R}} (xy - x^2) dx + x^2 y \, dy$$

along the curve C : $x=1,\ y=x,\ y=0,$ Evaluate : $\iint (\nabla \times \overline{\mathbb{F}}) \cdot \hat{n} \ ds,$

(b)



where $\overline{F} = (x - y)\overline{i} - (x^2 + yz)\overline{j} - 3xy \overline{k}$ and S is the surface of the cone $z = 4 - \sqrt{x^2 + y^2}$, above the xoy plane.

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Prove that : (c)

$$\iint\limits_{s} \ (\phi \nabla \Psi - \Psi \nabla \phi). \, d\overline{S} = \iiint\limits_{v} \ (\phi \nabla^{2} \Psi - \Psi \nabla^{2} \phi) \, dV$$

f(z) = u + iv

Show that the function : 7. (a)

[4]

with constant modulus and constant amplitude is constant in each case.

Evaluate : (b)

the bilinear transformation which maps the points:

$$z = 1, i, 2i$$

onto the points w = -2i, 0, 1 respectively.

$$f(z) = u$$

is analytic, find f(z), if

or
$$f(z) = u + iv$$

$$u - v = x^2 - y^2 - 2xy$$

$$f(z) = u + iv$$

$$f(z) = 0$$

$$f(z$$

(b) Evaluate: [4]

 $\oint_C \frac{(z^2 + \cos^2 z)}{\left(z - \frac{\pi}{4}\right)^3} dz,$

where C is circle |z| = 1.

(c) Find the map of the straight line y = x under the transformation

 $W = \frac{z - 1}{z + 1} \tag{4}$

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X.