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S.E. (Computer/IT Engineering) (Second Semester)

EXAMINATION, 2017

ENGINEERING MATHEMATICS III

(2015 Course)

Time: Two Hours

Maximum Marks : 50

N.B. :- (i) Neat diagrams must be drawn wherever necessary.

- (ii) Figures to the right indicate full marks.
- (iii) Your answers will be valued as a whole.
- (iv) Use of electronic pocket calculator is allowed.
 - (v) Assume suitable data, if necessary.
- 1. (a) Solve any two:
 - (i) $\frac{d^2y}{dx^2} + 3\frac{dy}{dx} + 2y = 2e^{ex}$
 - (ii) (D² + 4D + 4)y = $x^{-3} e^{-2x}$
 - (iii) $x^2 \frac{d^2y}{dx^2} 3x \frac{dy}{dx} + 5y = x^2 \sin(\log x)$
 - (b) Find the Fourier transform of :

$$f(x) = 1, |x| \le 1$$

$$= 0, |x| > 1$$

and evaluate $\int_0^\infty \frac{\lambda \cos \lambda x}{\lambda} d\lambda$.

[4]

- 2. (a) An inductor of 0.5 henries is connected in series with a registor of 6 ohms, a capacitor of 0.02 farads, a generator having alternative voltage given by 24 sin 10 t, t > 0 and switch k. Set up a differential equation for this circuit and find charge at time t. [4]
 - (b) Solve any one of the following: [4]
 - i) Find $z\{f(k)\}$, where $f(k) = 3^k, k < 0$ = $2^k, k > 0$
 - (ii) Find:

$$z^{-1}\left\{\frac{z^2}{z^2+1}\right\}$$

by using inversion integral method.

(c) Solve the following difference equation

$$y(k + 2) - 5y(k + 1) + 6y(k) = 36$$

 $y(0) = y(1) = 0$

 (a) Calculate the first four central moments from the following data and hence find β, and β,: [4]

Х	0	1	2	3	4	5	6
f	5	15	17	25	19	14	5

(b) Fit a straight line to the following data by least square method : [4]

					20	
y	12	15	17	22	24	30

- (c) The number of breakdowns of a computer in a week is a Poisson variable with $\lambda = np = 0.3$. What is the probability that the computer will operate : [4] with no breakdown and at the most one breakdown in a week. (iii) (a) The average test marks in a particular class is 79 and standard deviation is 5. If the marks are normally distributed, how many students in a class of 200, did not receive marks between
- 75 and 82. Given z = 0.8. Area = 0.2881 and z = 0.6. Area = 0.2257. [4]
 - (b) An insurance agent accepts policies of 5 men of identical age and in good health. The probability that a man of this age will be alive 30 years hence is 2/3. Find the probability that in 30 years : [4]
 - (i) all five men and
 - at least one man will be alive.
 - The two variables x and y have regression lines : (c) [4] 3x + 2y - 26 = 0 and 6x + y - 31 = 0

Find:

5.

- (i) the mean values of x and v and
- correlation coefficient between x and y. (ii)
- (a) Find the directional derivative of a scalar point function $\phi = xy^2 + yz^3$ at (2, -1, 1) in the direction of a vector 4i + 2i + 4k[4]

[5252]-566 3 P.T.O. (b) Show that the vector field:

$$\overline{F} = (6xy + z^3)i + (3x^2 - z)i + (3xz^2 - y)k$$

is irrotational and hence find a scalar potential function ϕ such that $\overline{F} = \nabla \phi$. [4]

(c) Find the work done by the vector field: [5]

$$\vec{F} = (x^2 - yz)i + (y^2 - zx)j + (z^2 - xy)k$$

in moving a particle of unit mass from (1,1,1) to $(2,-1,\ 2)$.

- 6. (a) Find the directional derivative of a scalar point function φ = xy - z² + 2xz at (1, 0, 2) in the direction of 4i - j + 2k. [4]
 - b) Show that (any one):
 - (i) $\nabla \left(\frac{\overline{a}.\overline{r}}{r^a}\right) = \frac{\overline{a}}{r^a} \frac{n(\overline{a}.\overline{r})\overline{r}}{r^{a+2}}$, where \overline{a} is a constant vector.

$$(ii) \quad \nabla^2 \left(\nabla \cdot \frac{\overline{r}}{r^2} \right) \; = \; \frac{2}{r^4} \; .$$

- (c) Evaluate the integral $\int_{c}^{\overline{F}} \cdot d\overline{r}$, along the curve x = 2t, y = t, z = 3t from t = 0 to t = 1, where $\overline{F} = 3x^{2}t + (2xz y)j + zk$.
- **7.** (a) If :

$$u = -2xy + \frac{y}{x^2 + y^2},$$

find v such that f(z) = u + iv is analytic. Determine f(z) in terms of z.

(b) Evaluate $\oint_{c} \frac{e^{z}}{(z+1)(z+2)} dz$, where c is the contour

$$|z + 1| = \frac{1}{2}$$
. [5]

(c) Find the Bilinear transformation which maps the point -i, 0, 2 + i of the z-plane onto the points 0, -2i, 4 of the w-plane. [4]

Or

8. (a) If:

$$u = \frac{1}{2}\log(x^2 + y^2),$$

find v such that f(z) = u + iv is analytic. Determine f(z) in terms of z.

b) Evaluate $\oint_C \frac{\sin \pi z^2 + 2z}{(z-1)(z-2)} dz$, where c is the circle |z| = 4.

[5]

(c) Find the image of the circle $(x-3)^2+y^2=2$ under the transfromation $w=\frac{1}{z}$.